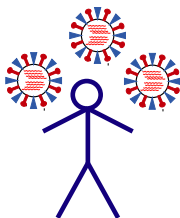


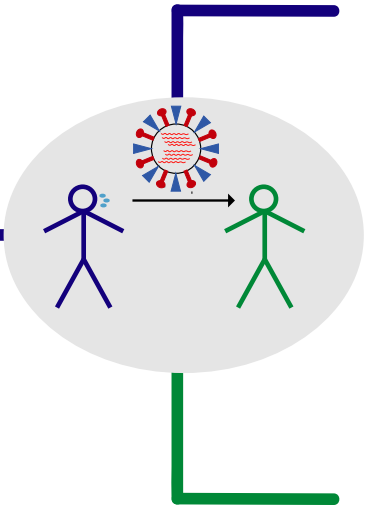
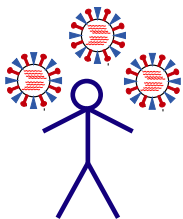
Tracking the evolution of pathogens over time

Nicola F. Müller

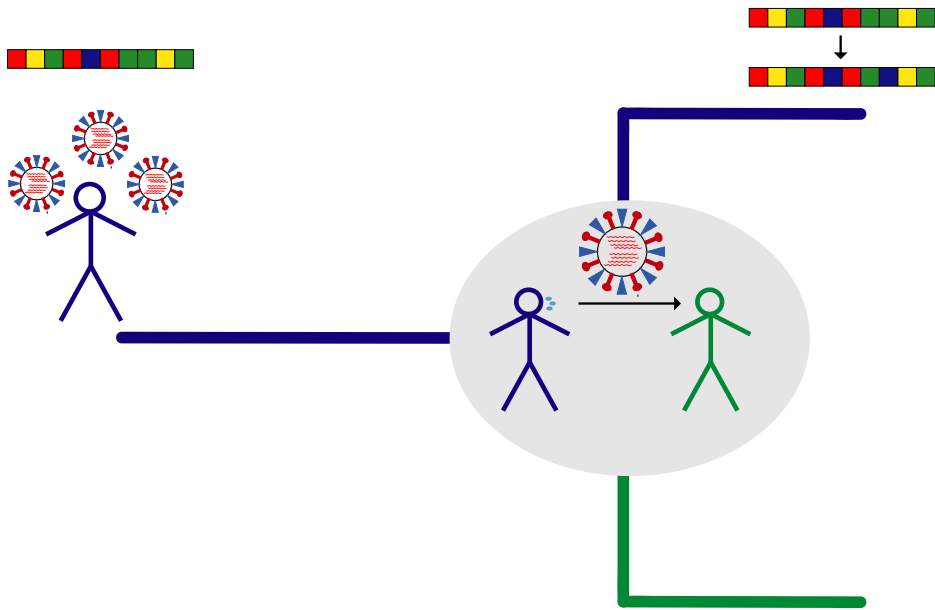
e-mail: nicola.mueller@ucsf.edu



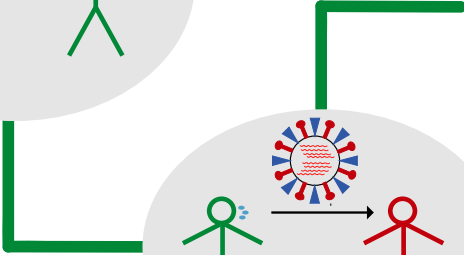
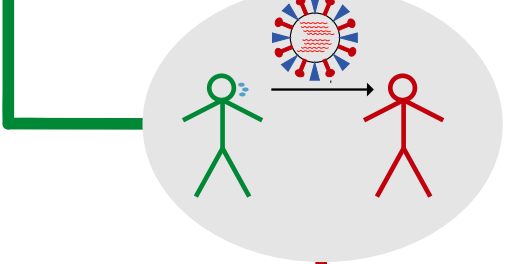
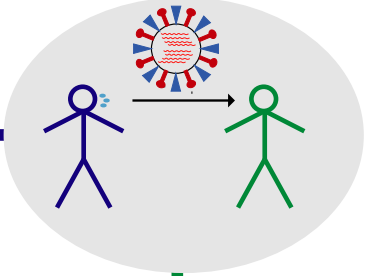
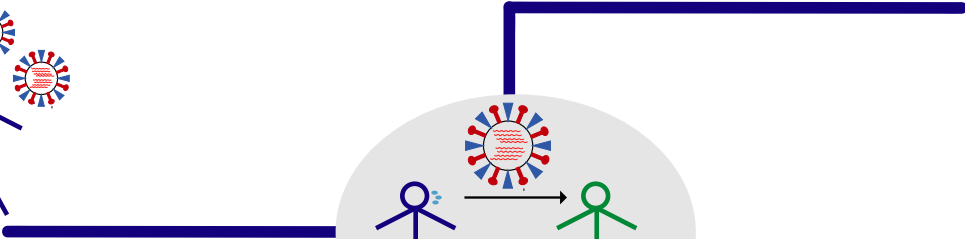
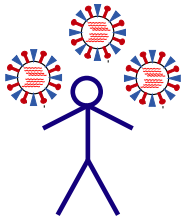
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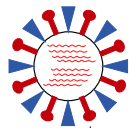
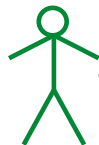
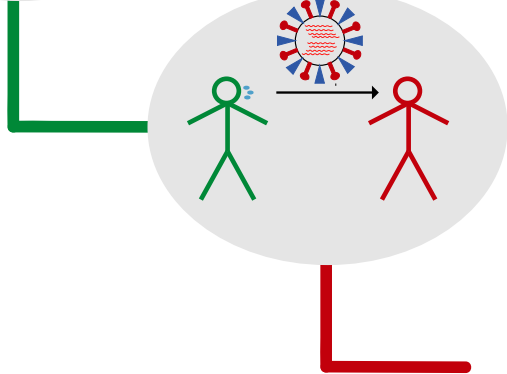
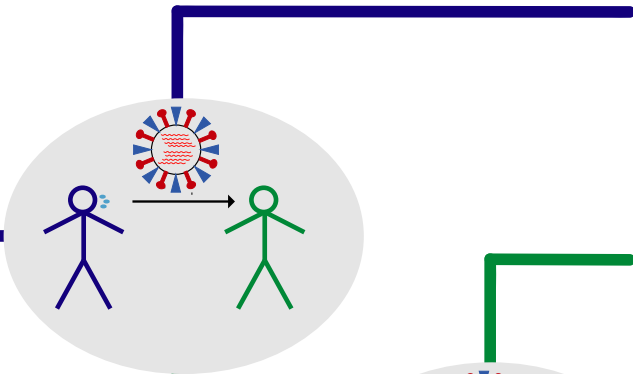
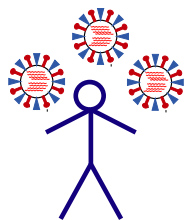
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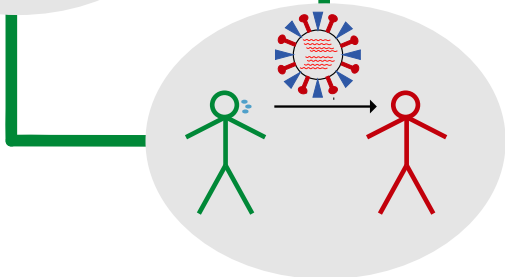
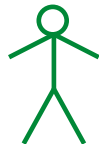
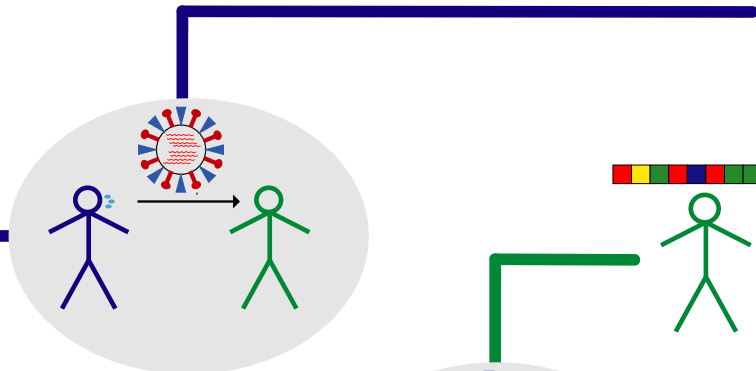
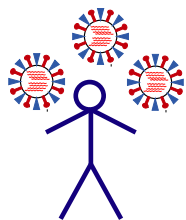
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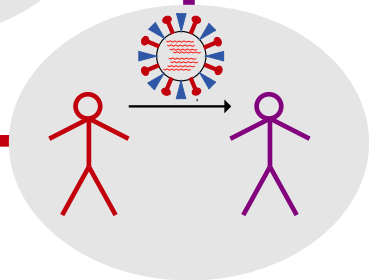
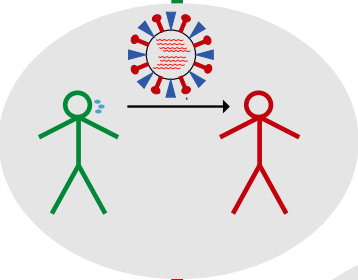
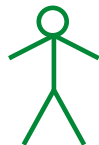
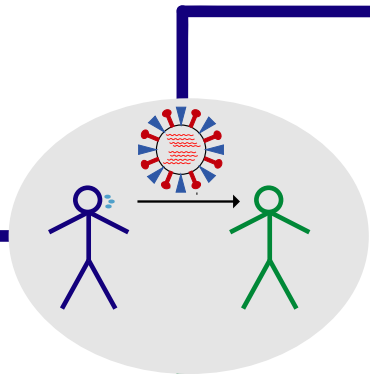
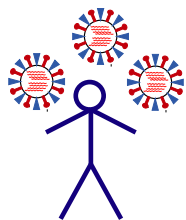
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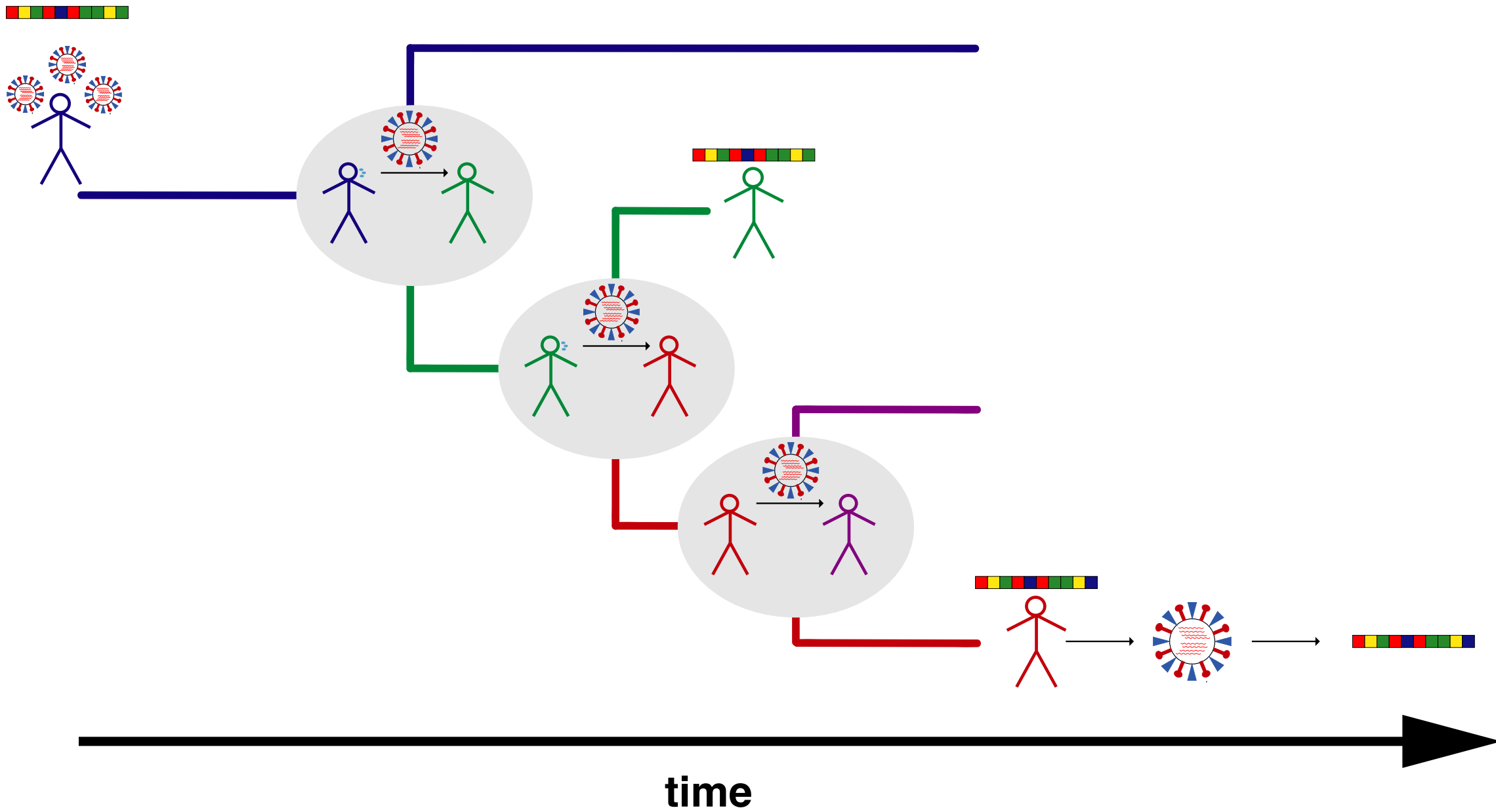
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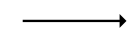
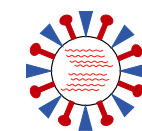
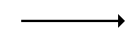
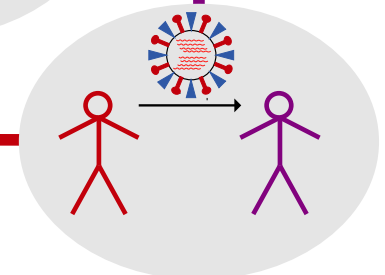
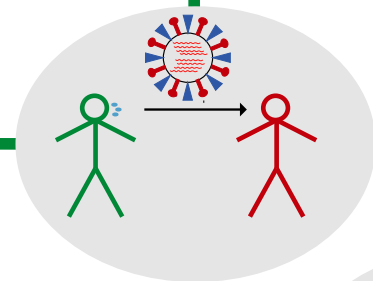
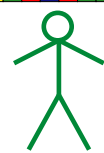
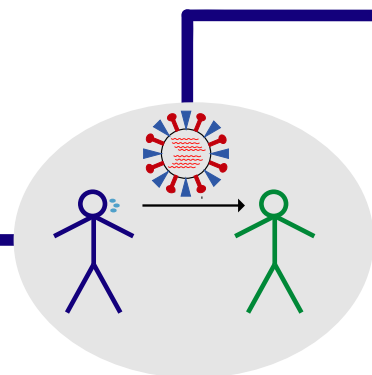
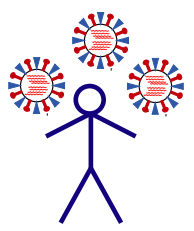


time

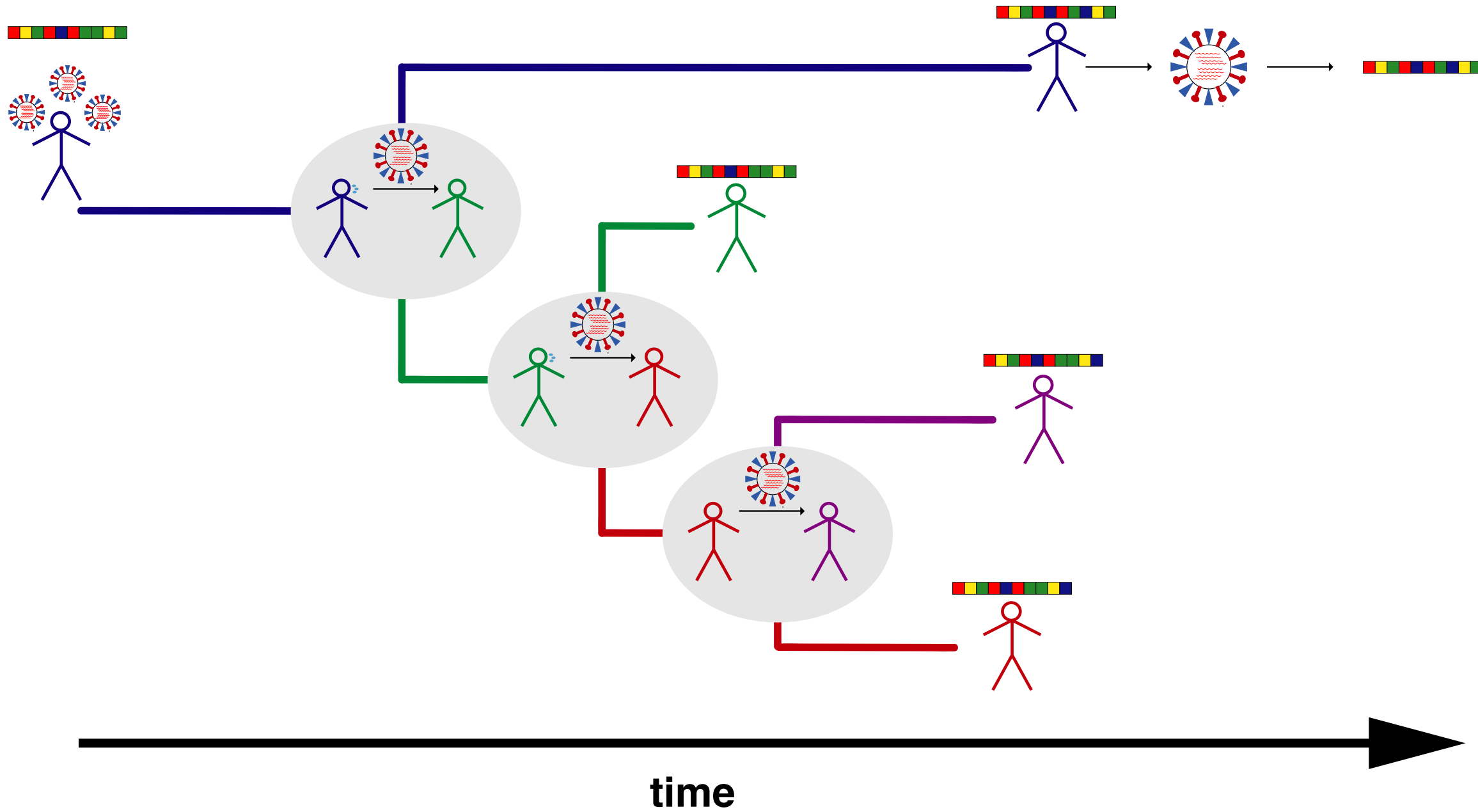


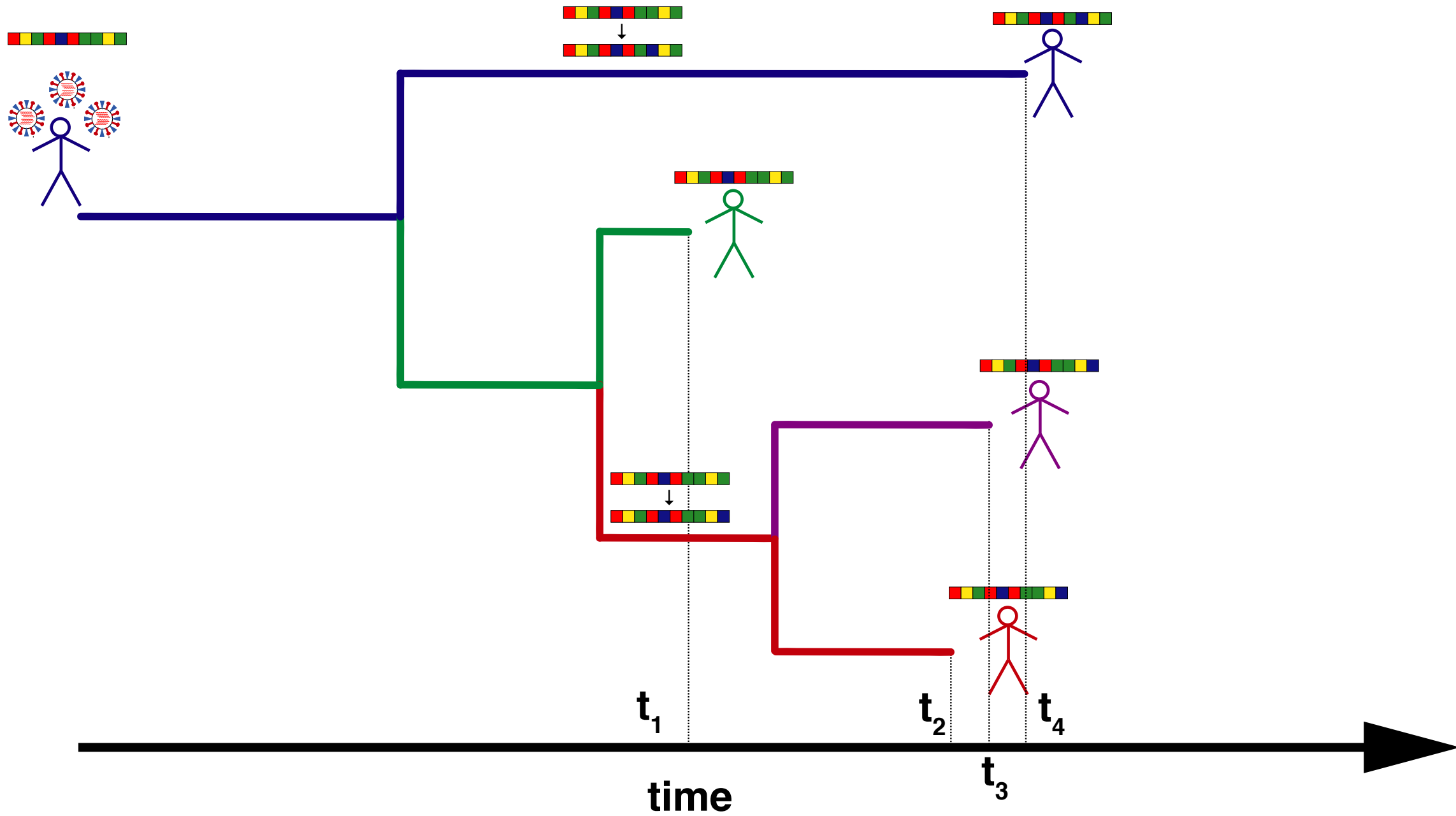
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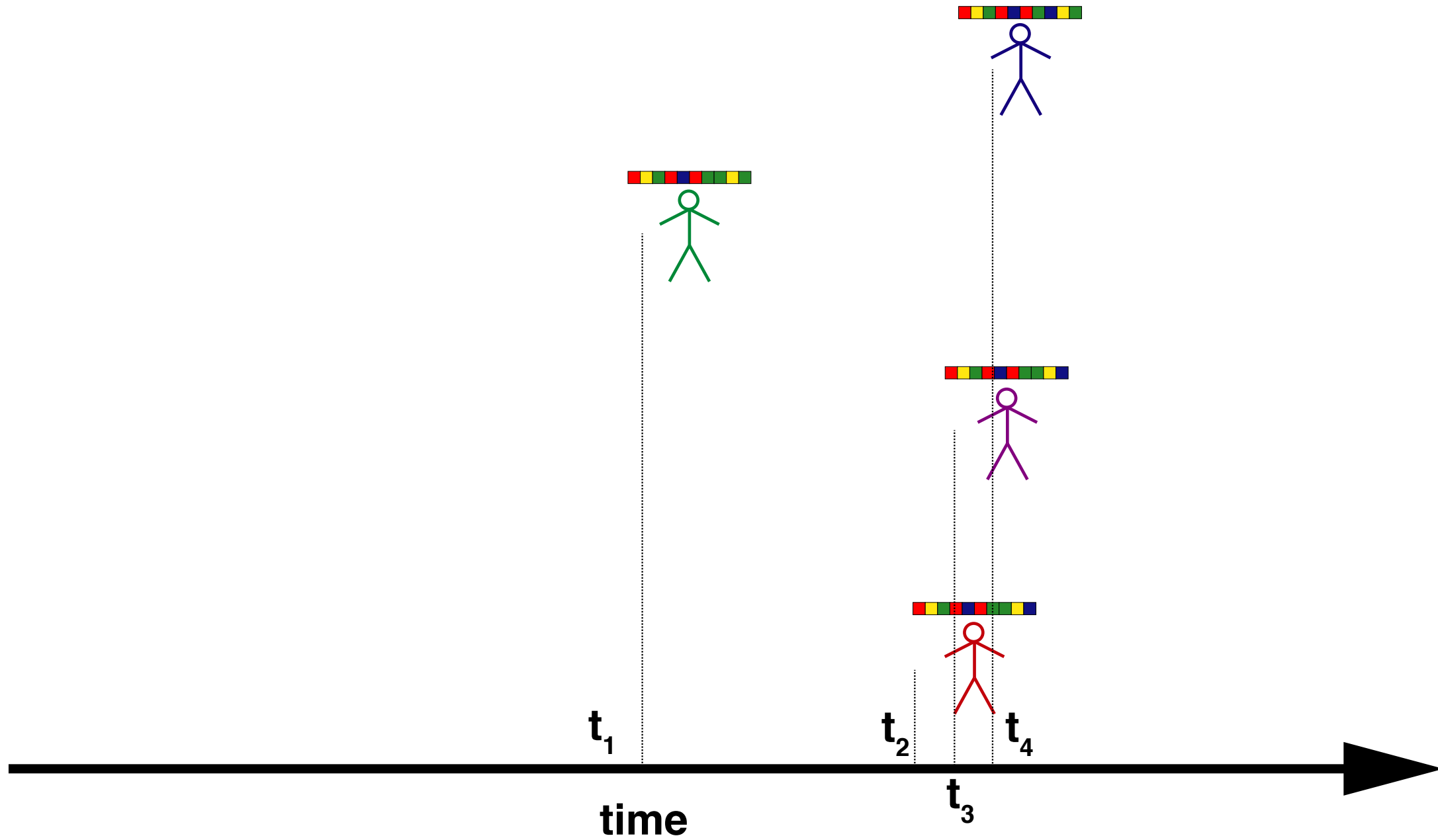




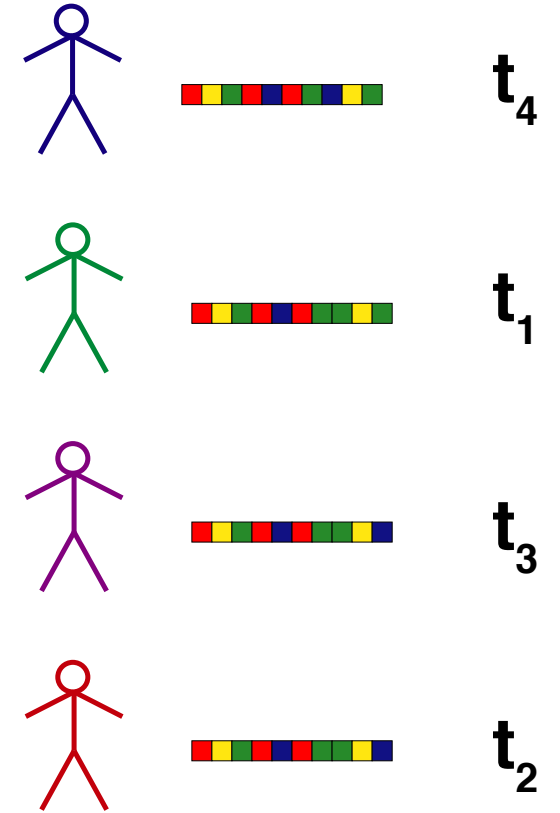
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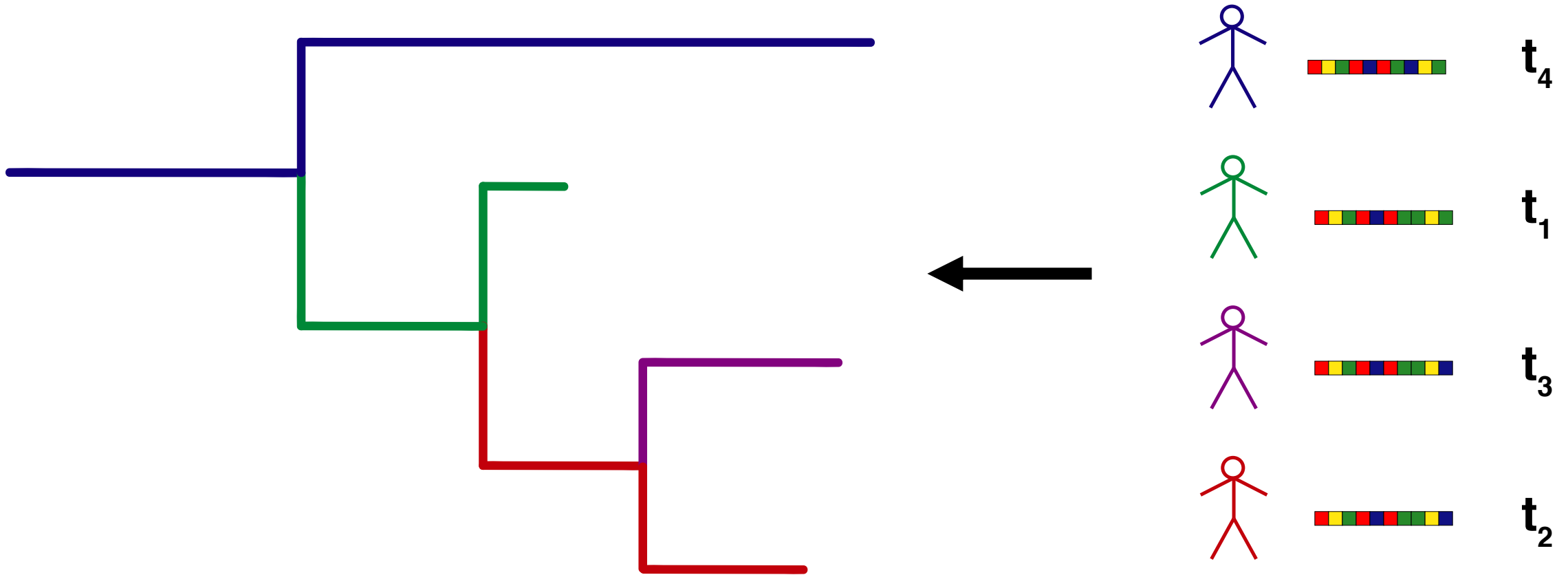




Our data: We know who was infected with which pathogen and sequence and when they were sampled



Phylogenetics allows us to infer the shared ancestral history of the different pathogens



Bayesian phylogenetics allows us to jointly infer the phylogenetic trees, evolutionary and Demographics models

$$P(\text{Phylogenetic Tree} \mid \text{Genomic Data})$$

Bayesian phylogenetics allows us to jointly infer the phylogenetic trees, evolutionary and Demographics models

Tree generating models



$$P(\text{Tree} \mid \text{Data}) = \frac{P(\text{Tree} \mid \text{Model}) P(\text{Model})}{P(\text{Data})}$$

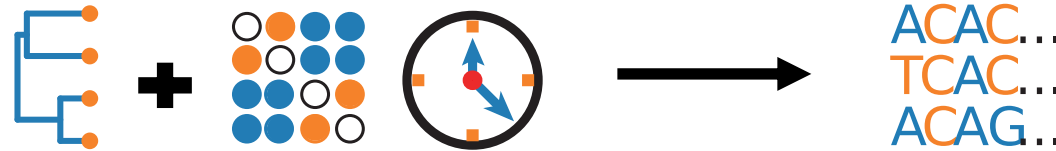
The equation represents the joint inference of the phylogenetic tree, evolutionary model, and demographic model. The numerator consists of the probability of the tree given the model and the probability of the model. The denominator is the probability of the data given the model and the tree.

Bayesian phylogenetics allows us to jointly infer the phylogenetic trees, evolutionary and Demographics models

Tree generating models



Model of sequence evolution



$$P(\text{Tree, Matrix, Clock} \mid \text{Sequence}) = \frac{P(\text{Sequence} \mid \text{Tree, Matrix, Clock}) P(\text{Tree} \mid \text{Coalescent}) P(\text{Coalescent}) P(\text{Matrix}) P(\text{Clock})}{P(\text{Sequence})}$$

Divergence Tree

individual_1/t 1

individual_2/t 2

individual_3/t 3

individual_4/t 3



individual_4/t 3



individual_3/t 3

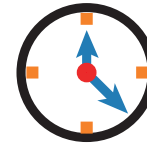
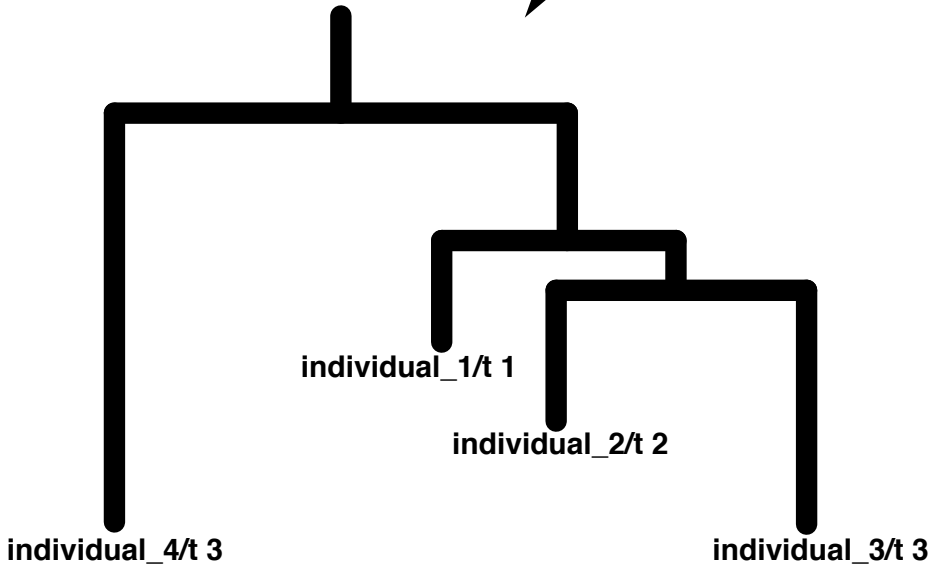
individual_1/t 1

individual_2/t 2

Time Tree

past

present





Site models describe the relative change across nucleotides and positions in the alignment and consist of several parts.

- **Substitution models** describe how fast/slow the change from one to another nucleotide happens compared to others
- **Gamma rate heterogeneity + invariant site models** describe how fast/slow some sites in an alignment change bases compared to others
- **Codon positions models** allow for some codon positions to evolve faster/slower than others



Substitution models describe how fast/slow the change from one to another nucleotide happens compared to others

BEAUi 2:

Partitions Tip Dates **Site Model** Clock Model Priors MCMC

Gamma Site Model

Substitution Rate 1.0 ? e ☐ estimate

Gamma Category Count 0 ?

Proportion Invariant 0.0 ? e ☐ estimate

Subst Model JC69 ?



Gamma rate heterogeneity + invariant site models describe how fast/slow some sites in an alignment change bases compared to others

BEAUi 2:

Partitions Tip Dates Site Model ? Clock Model Priors MCMC

Gamma Site Model ?

Substitution Rate 1.0 ? e ☐ estimate

Gamma Category Count 0 ?

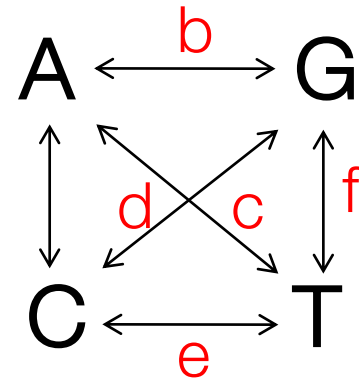
Proportion Invariant 0.0 ? e ☐ estimate

Subst Model JC69 ?



Substitution models allow to account for differences in nucleotide substitution rates.

Rate Matrix



Equilibrium Base Frequencies

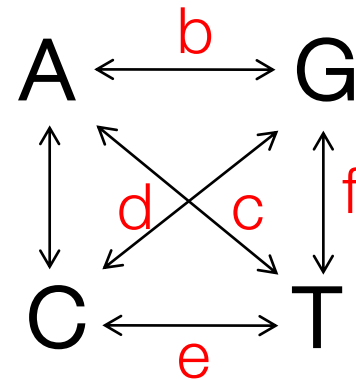
$$\pi_A + \pi_C + \pi_G + \pi_T = 1$$



Substitution models allow to account for differences in nucleotide substitution rates.

Rate Matrix

Equilibrium Base Frequencies



$$\pi_A + \pi_C + \pi_G + \pi_T = 1$$

JC

$$a=b=c=d=e=f$$

$$\pi_A = \pi_C = \pi_G = \pi_T$$

No I or G

0 free

parameters

HKY

$$a=c=d=f, b=e$$

$$\pi_A, \pi_C, \pi_G, \pi_T$$

No I or G

4 free

parameters

GTR

$$a, b, c, d, e, f$$

$$\pi_A, \pi_C, \pi_G, \pi_T$$

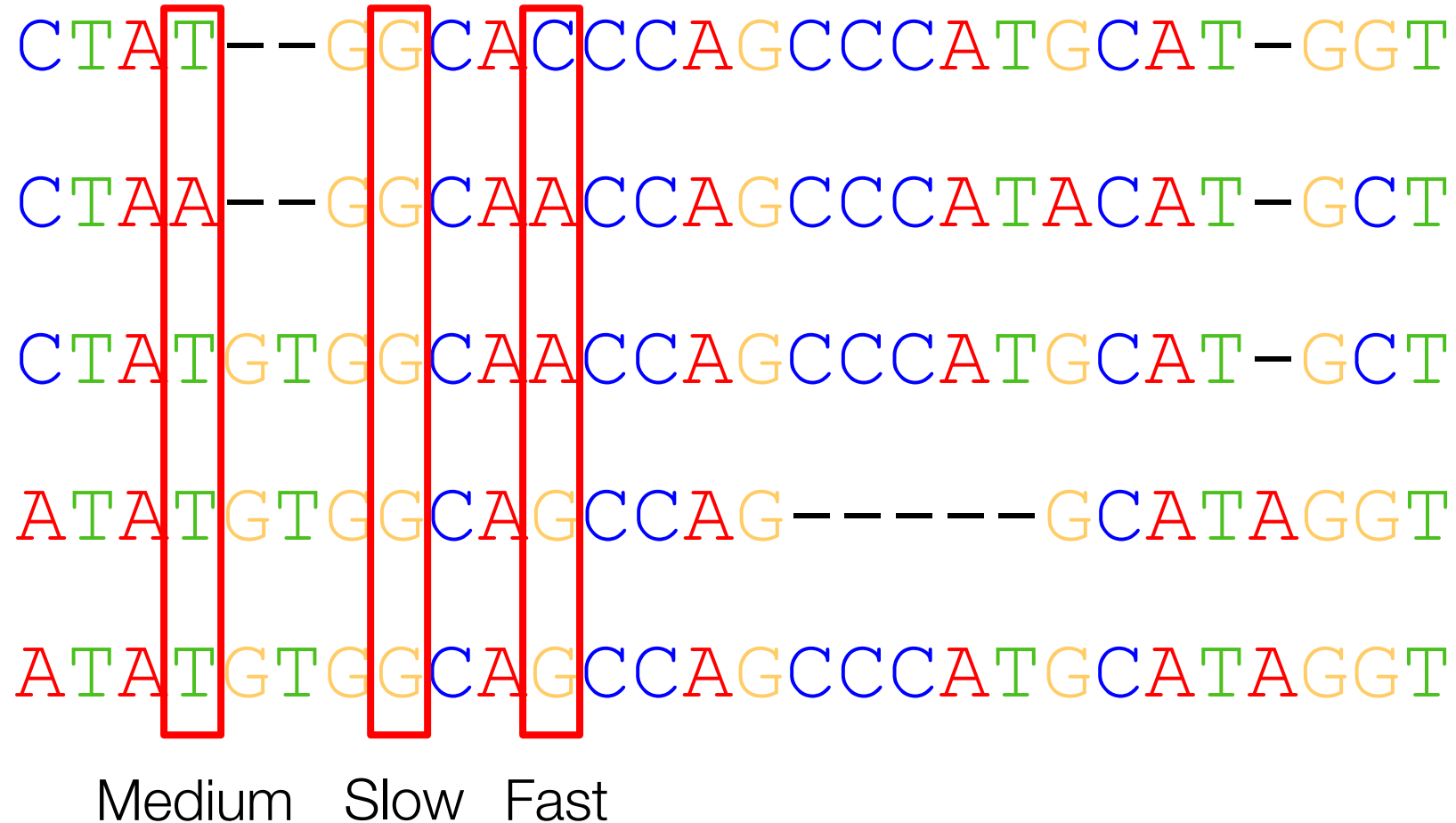
No I or G

8 free

parameters

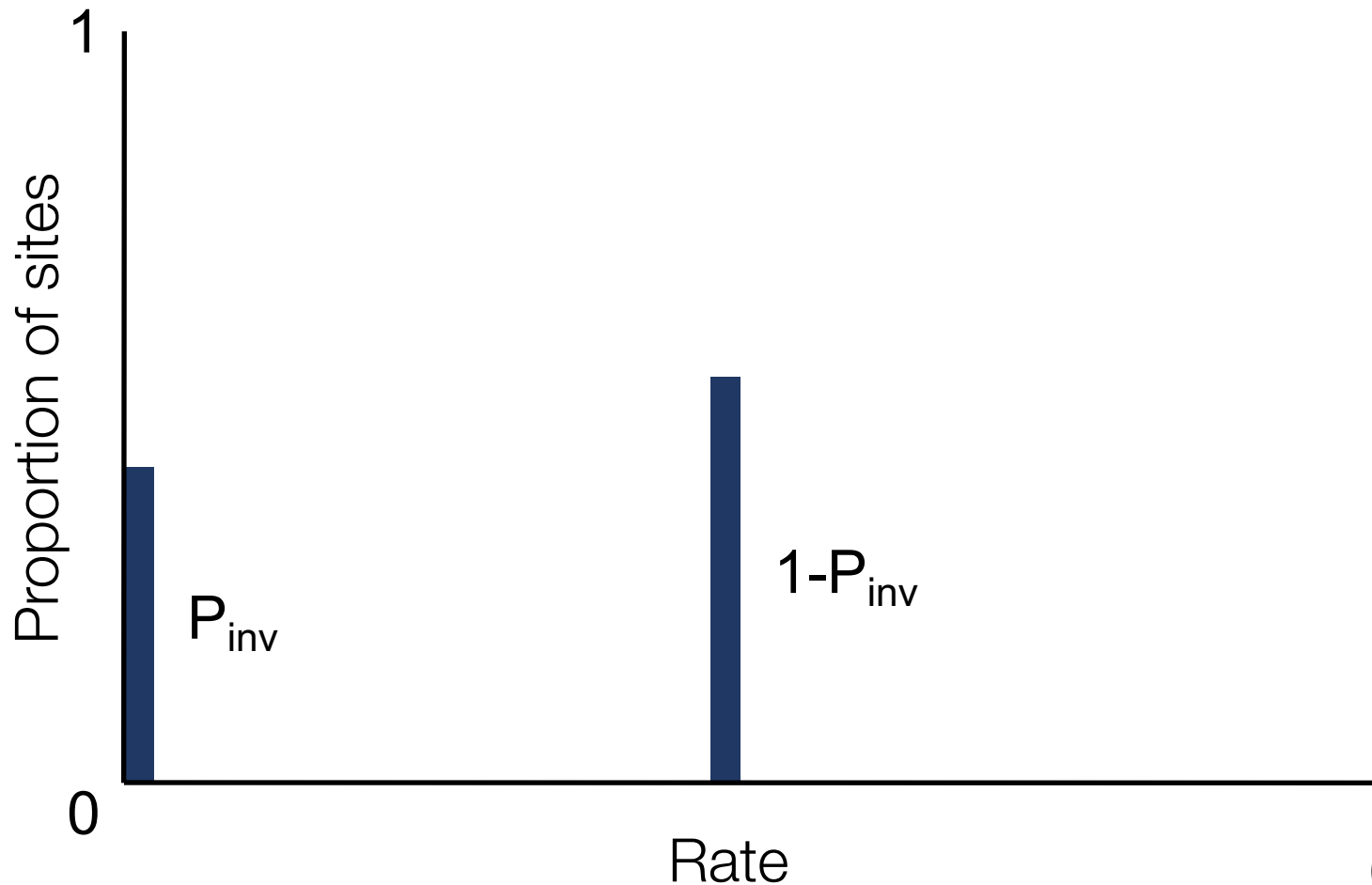


Some site in the alignment might be more flexible and therefore evolve less quickly.





Proportion of invariable sites account for sites that do not change (e.g., HKY+I).





Gamma rate heterogeneity + invariant site models describe how fast/slow some sites in an alignment change bases compared to others

BEAUi 2:

Partitions Tip Dates Site Model ? Clock Model Priors MCMC

Gamma Site Model ?

Substitution Rate 1.0 ? e ☐ estimate

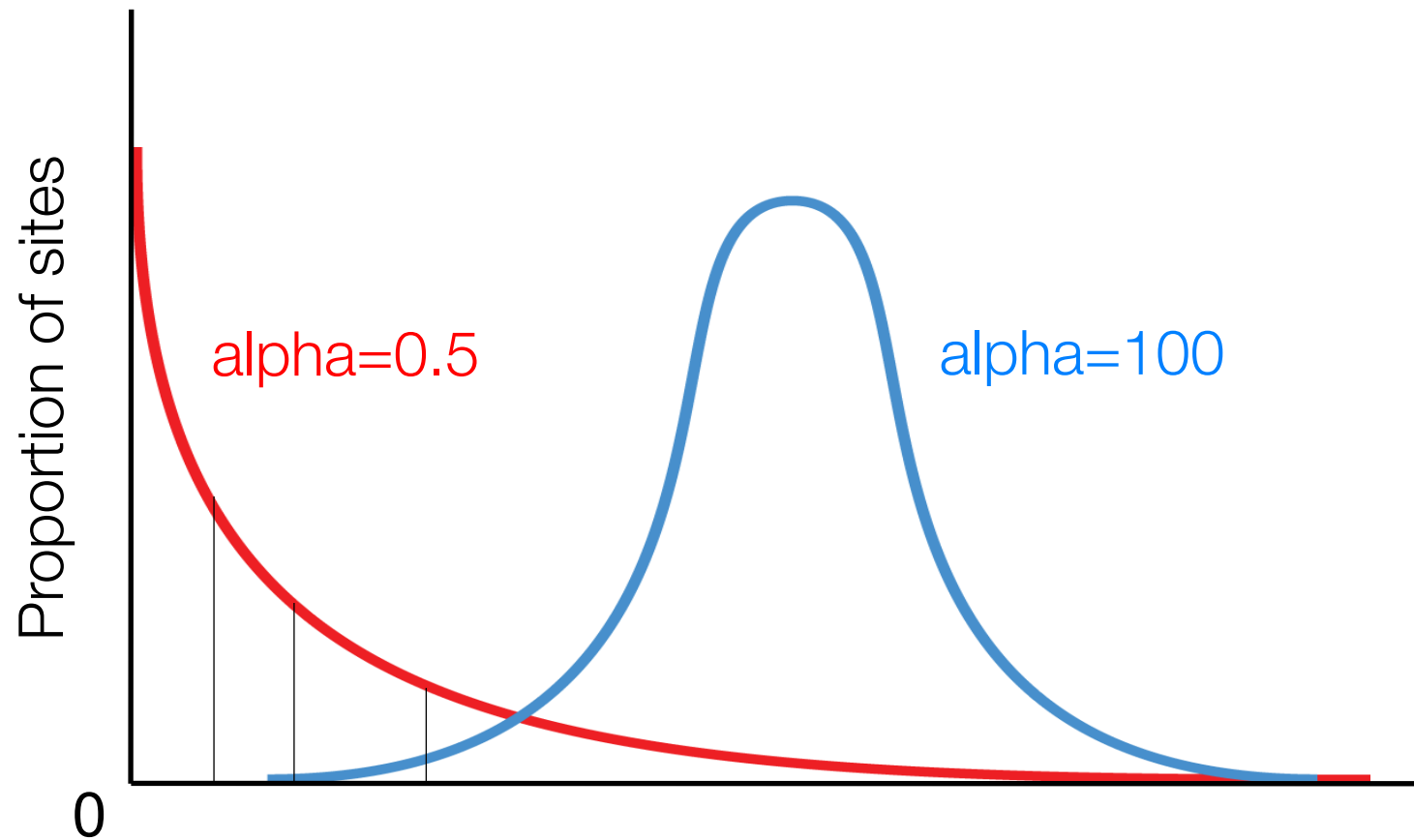
Gamma Category Count 0 ?

Proportion Invariant 0.0 ? e ☐ estimate

Subst Model JC69 ?



Gamma rate heterogeneity models account for rate differences across sites (e.g. HKY+G₄).





Gamma rate heterogeneity + invariant site models describe how fast/slow some sites in an alignment change bases compared to others

BEAUi 2:

Partitions Tip Dates Site Model ? Clock Model Priors MCMC

Gamma Site Model ?

Substitution Rate 1.0 ? e ☐ estimate

Gamma Category Count 0 ?

Proportion Invariant 0.0 ? e ☐ estimate

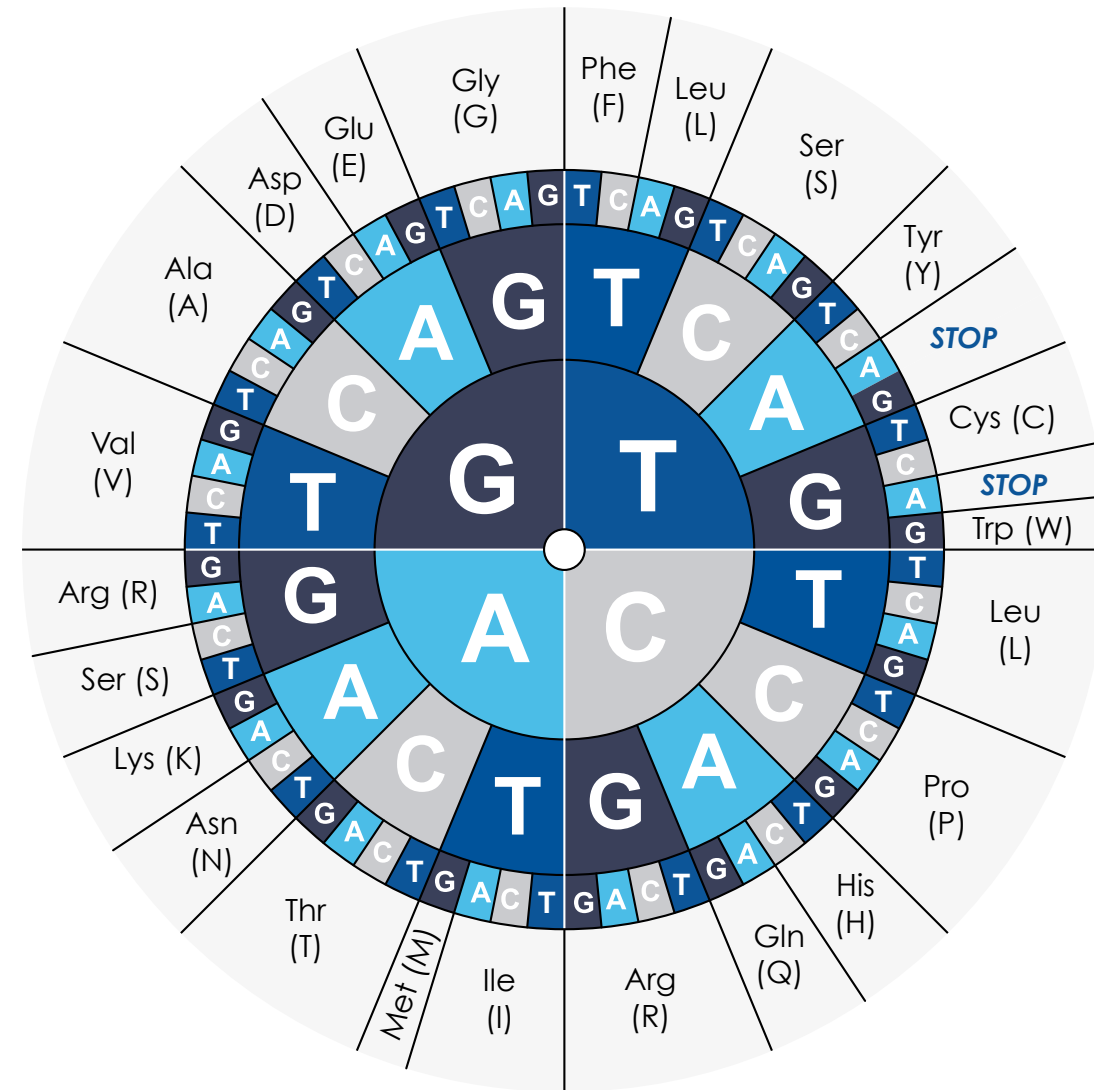
Subst Model JC69 ?



Genetic Code

Changes in the third codon position are far more likely to not affect the amino acid

- Splitting up the alignment into different codon positions and allow each having its own site model allows accounting for these differences



GENOMIC SEARCH ENGINE

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<http://bit.ly/mastermind-codon>



GENOMENON®
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Genetic Code

CTA (Leucine)

First position:

ATA (Isoleucine)

GTA (Valine)

TTA (Leucine)

Second position:

CCA (Proline)

CAA (Glutamine)

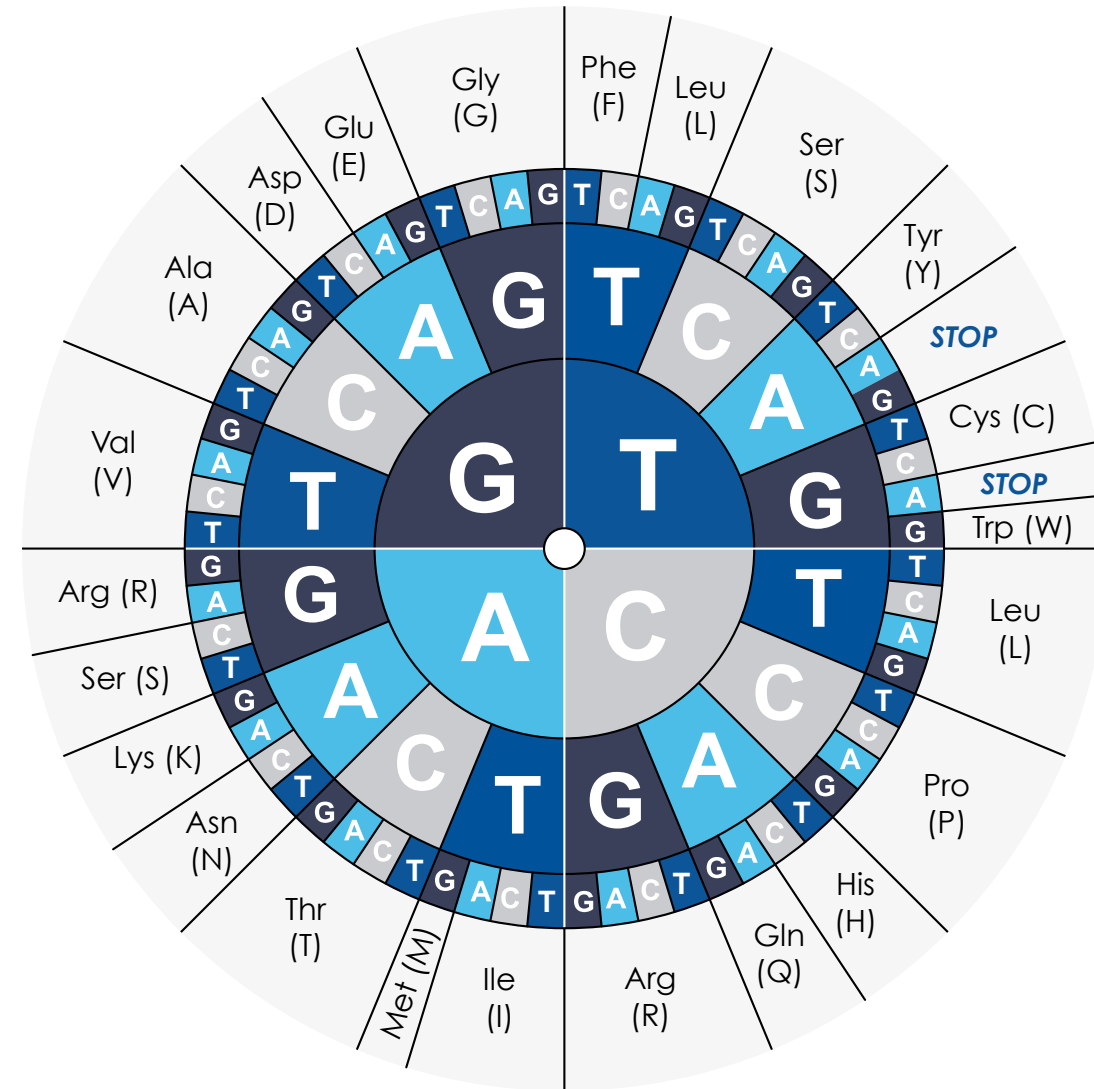
CGA (Arginine)

Third position:

CTC (Leucine)

CTG (Leucine)

CTT (Leucine)



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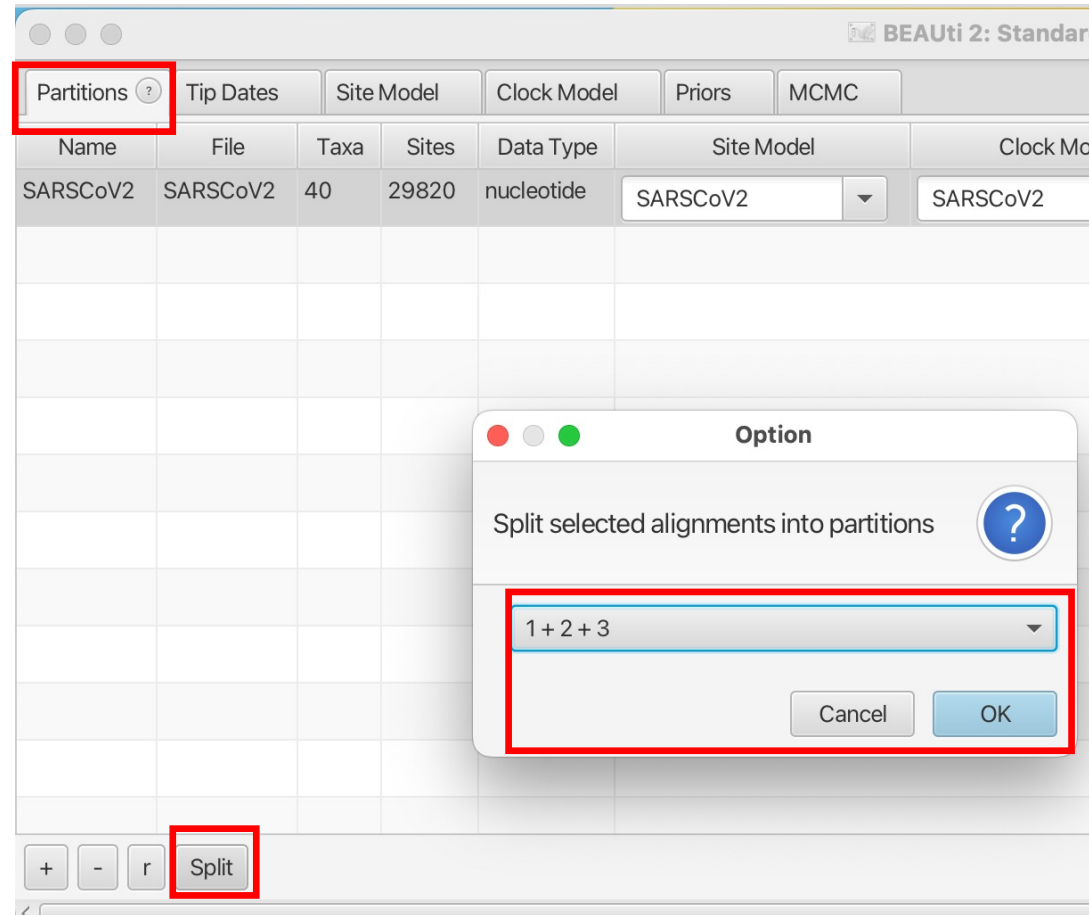


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<https://www.genomenon.com/codon-chart/>



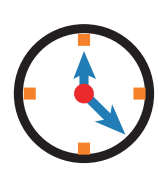
Codon positions models allow for some codon positions to evolve faster/slower than others



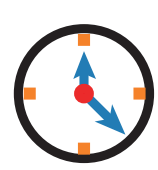


Practical considerations

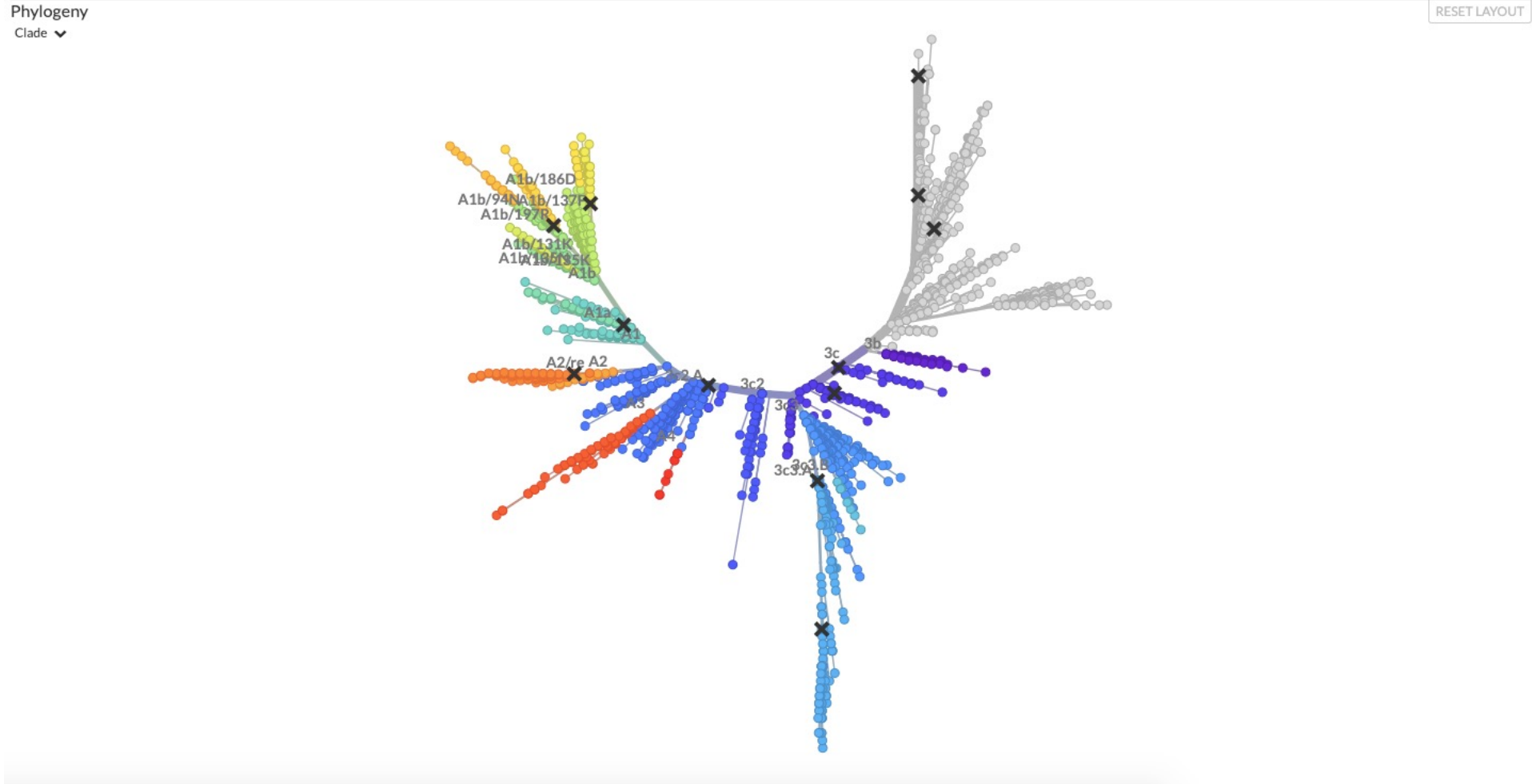
- Everything affects everything in Bayesian phylogenetics. Wrong evolutionary models lead to wrong trees, which leads to wrong population parameters.
- Overparameterization is better than under-parameterization. In doubt, use the more complex site model, such as a GTR+ model (Abadi et al., 2019, Nat. comm.)
- Never forget to account for rate heterogeneity (experience). Also, the JC69 model is hardly ever appropriate.



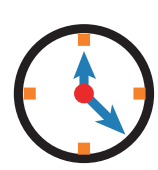
The molecular clock



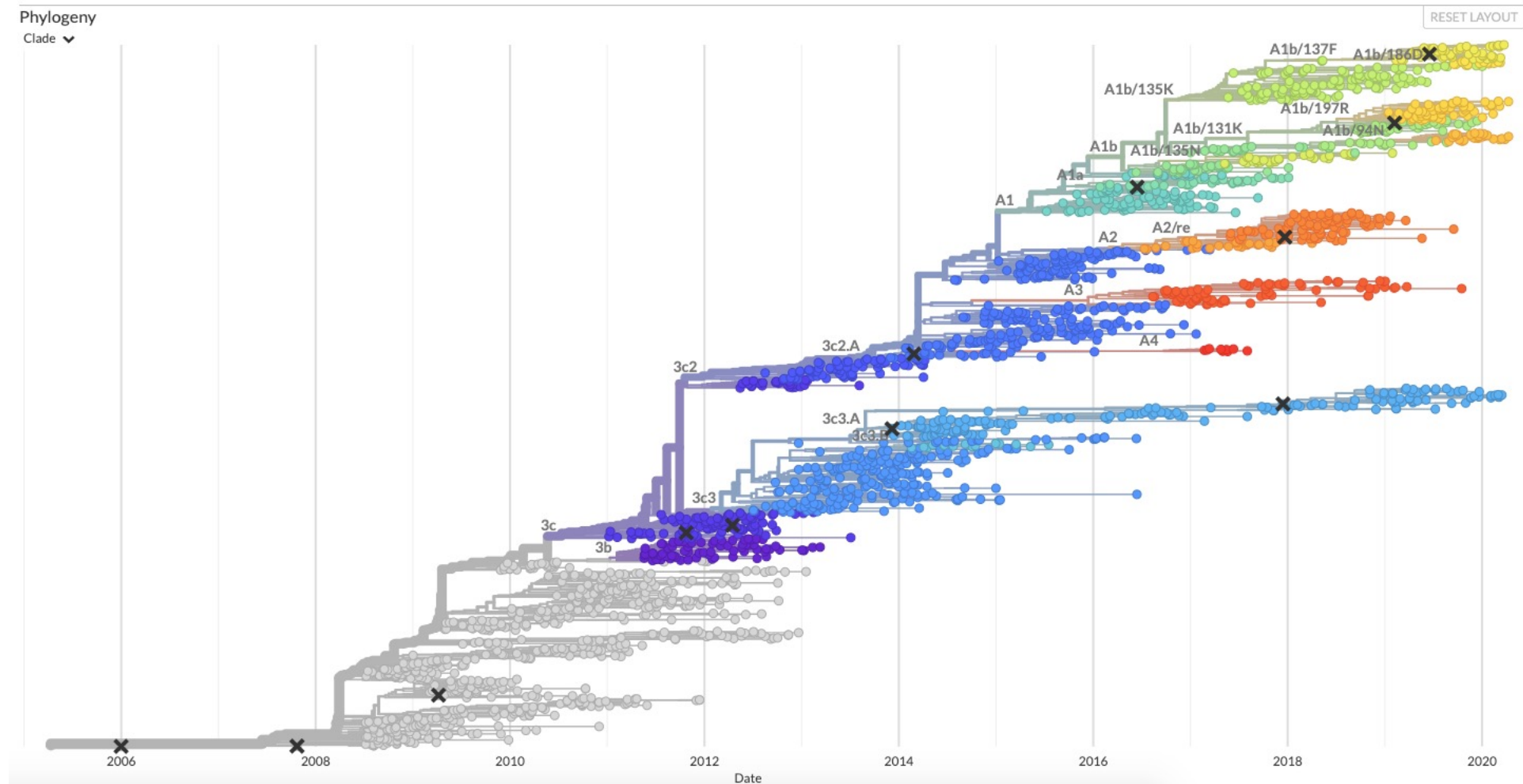
Using site models, we can get from alignments to divergence trees

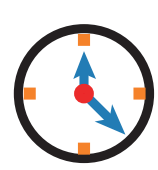




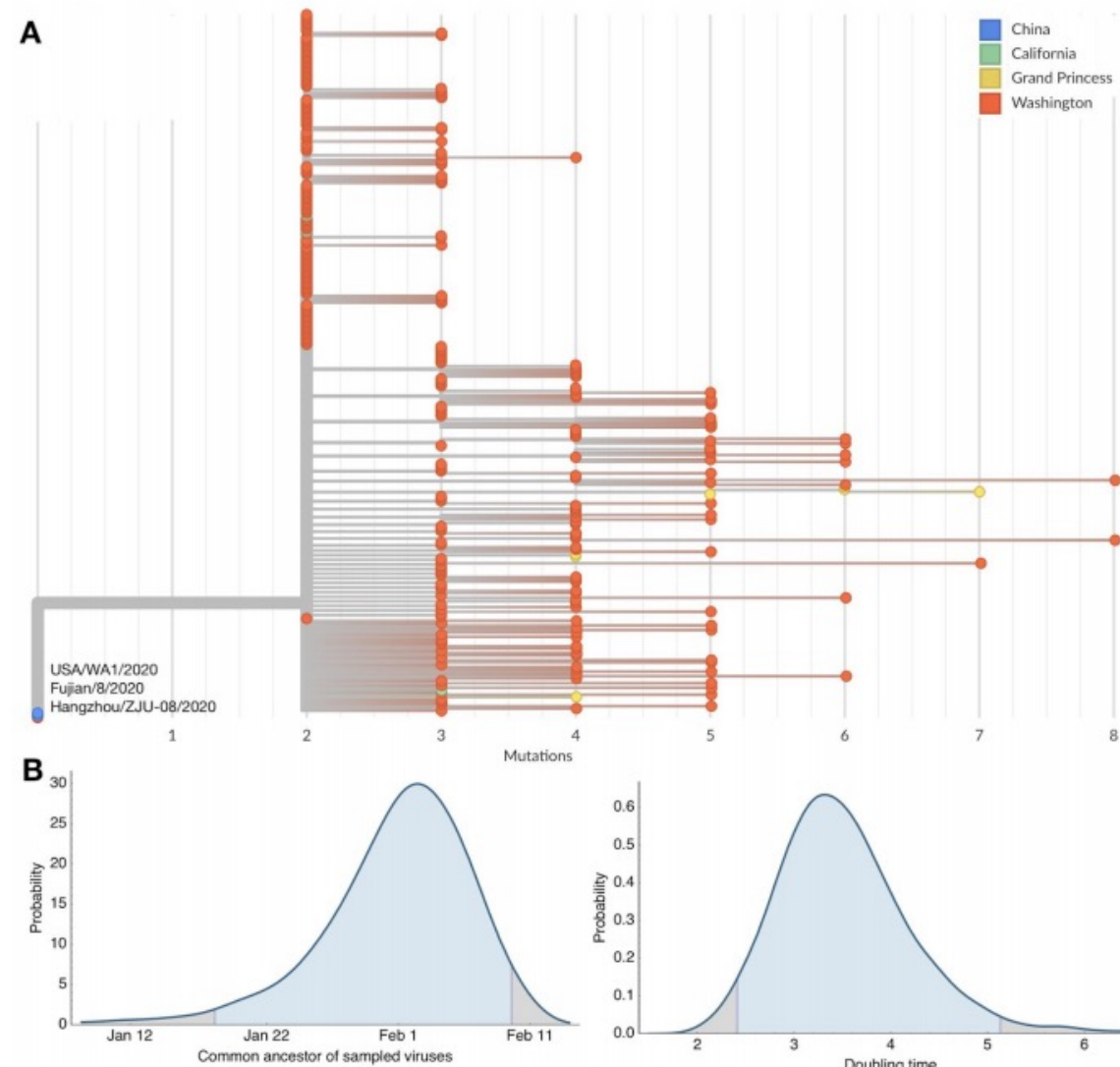


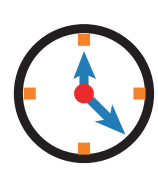
Molecular clocks bring us from divergence trees to time trees



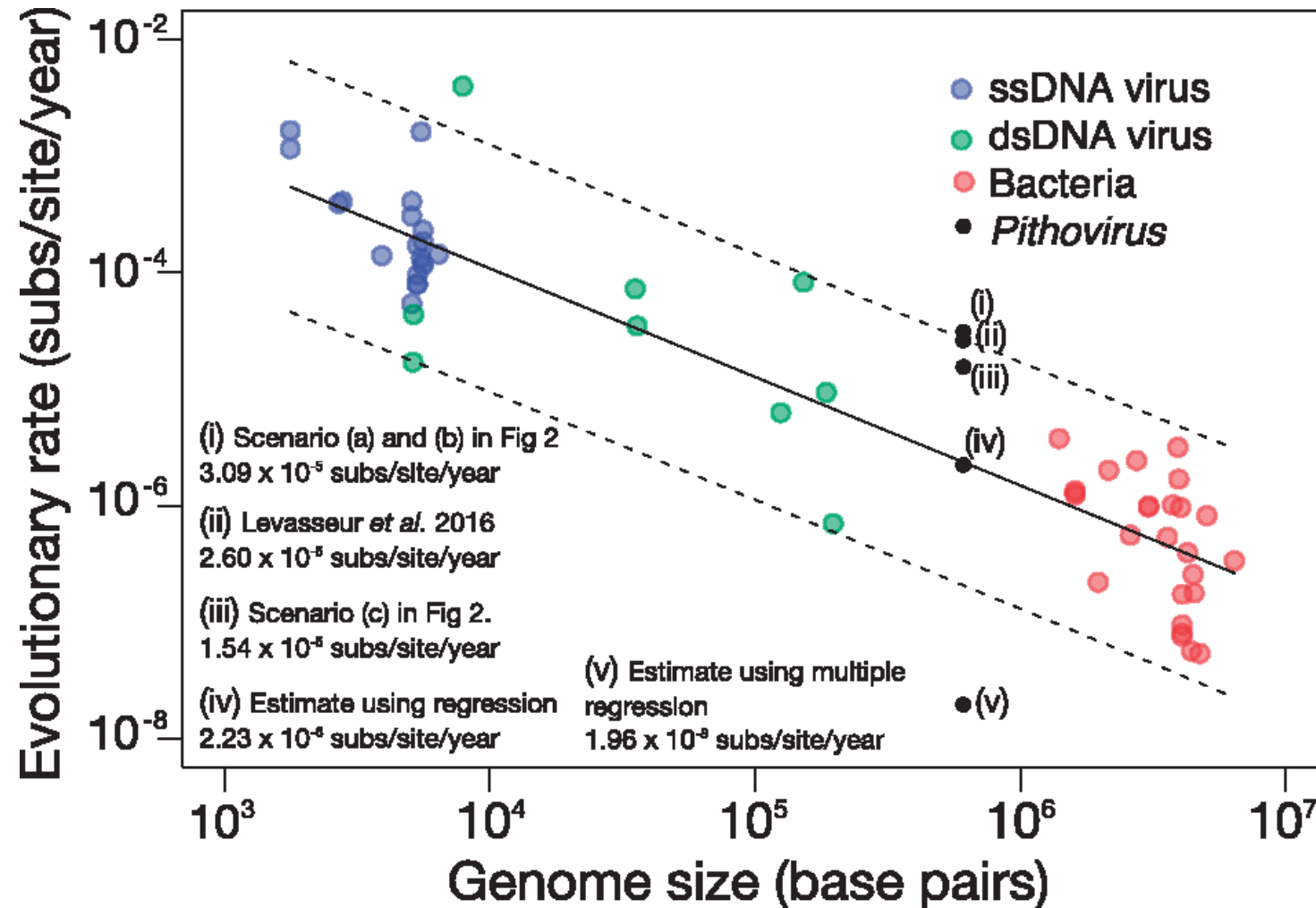


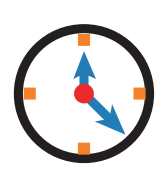
Evolutionary models can be used to estimate common ancestor times



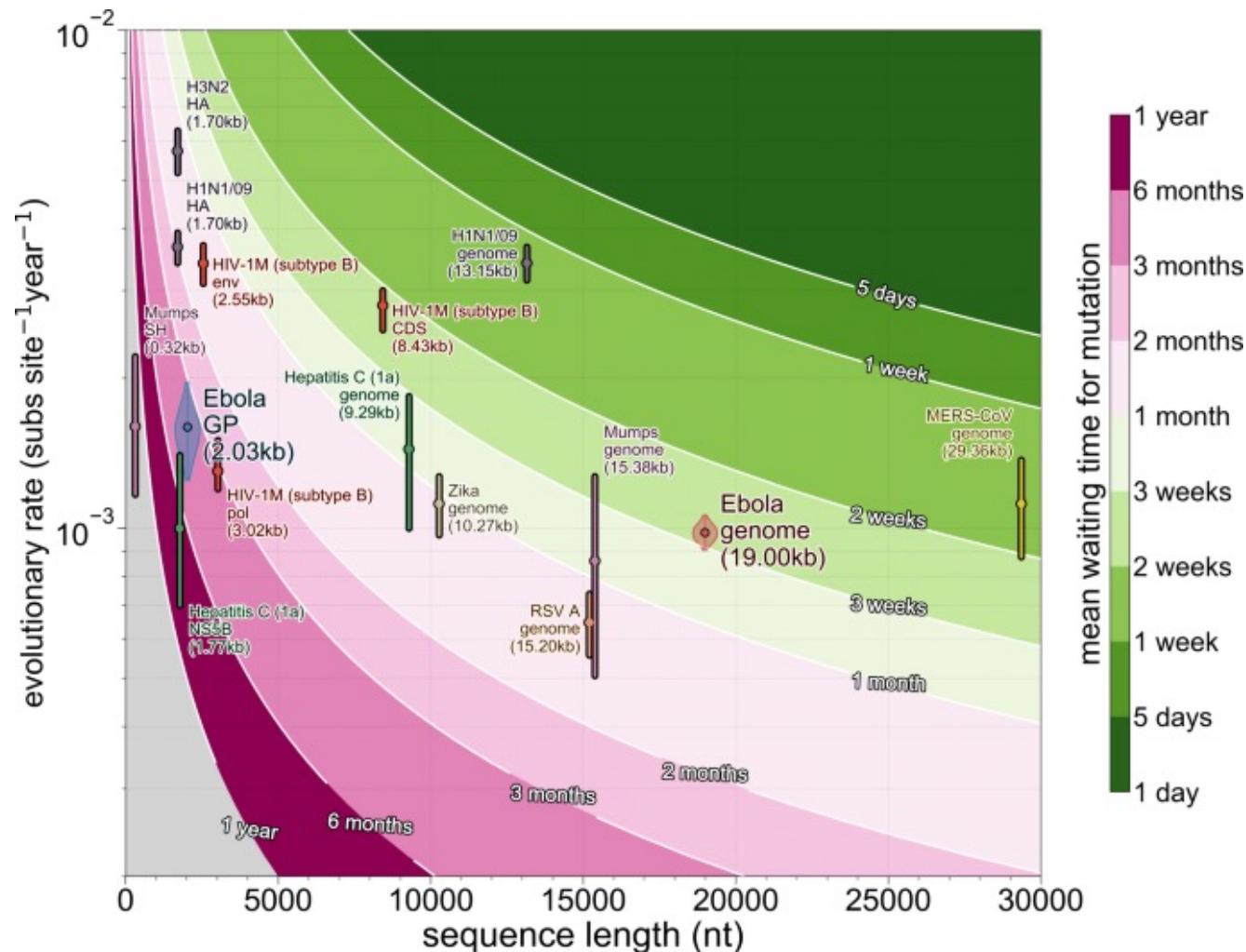


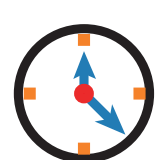
Different organisms have vastly different rates of evolution





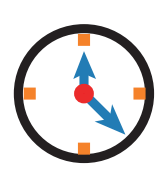
The time resolution is dependent on the size of the genome and the rate of evolution



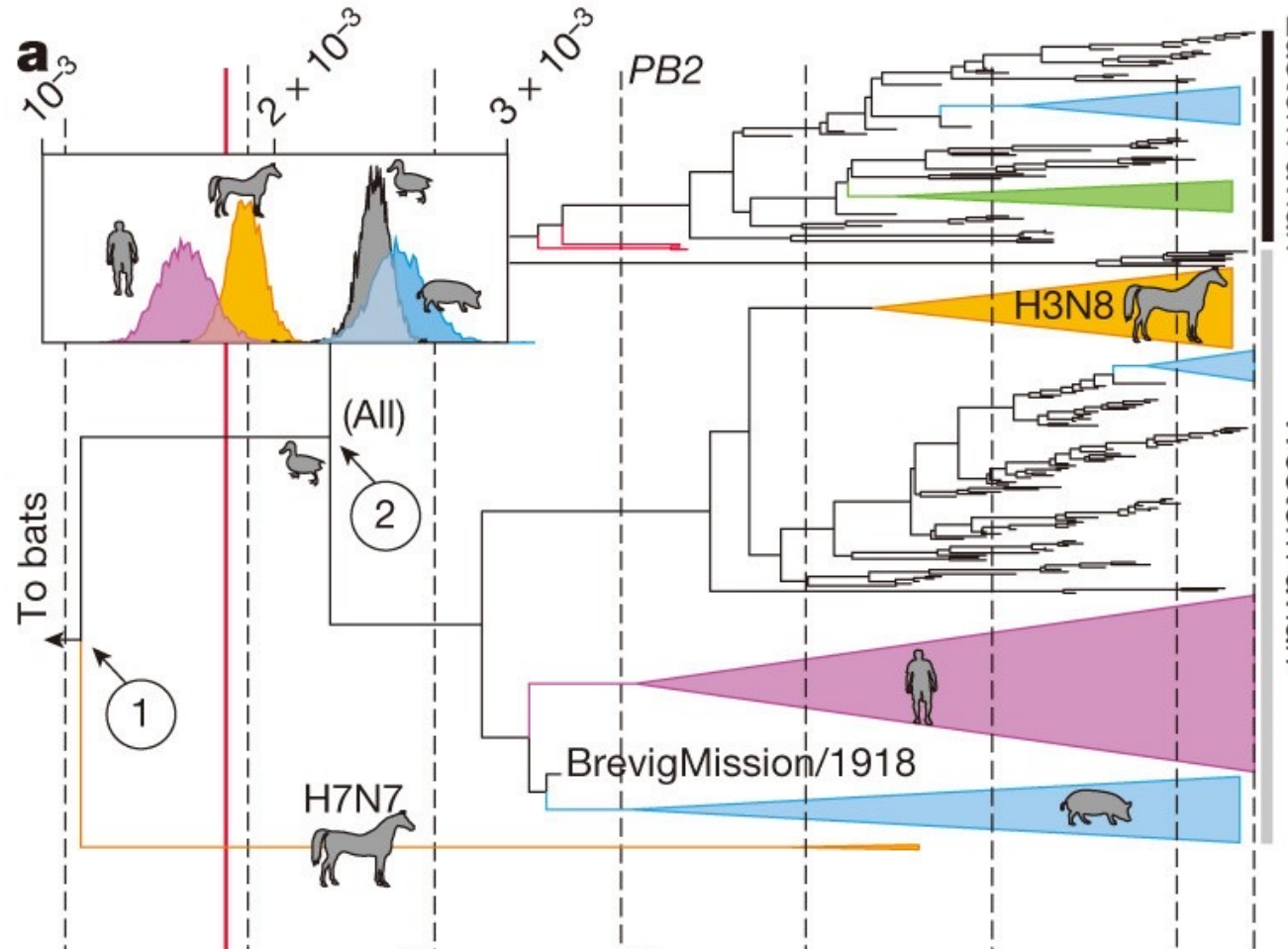


What is my clock rate? (from Holmes et al. 2016)

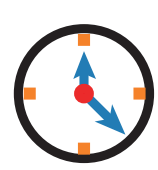
- **Mutation rate (short term, faster):** Error rate in replication.
- **Substitution rate (long term, slower):** Long term rate of evolution.
- **Evolutionary rate (=clock rate):** Measured rate of change. Result of mutation rate and population processes, such as selection. Typically sits between the mutation and substitution rate (The notation in BEAST is confusing with regards to what is what).



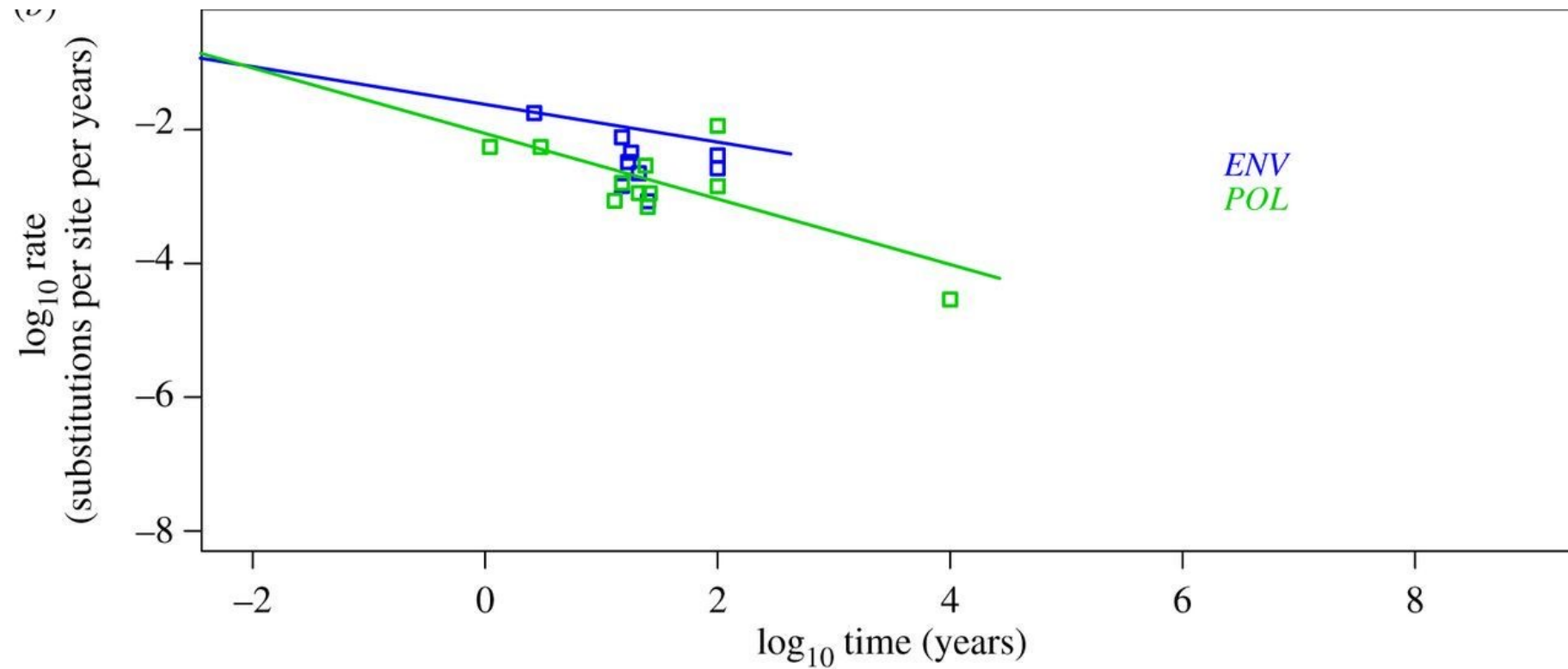
Rates of evolution can vary due to different hosts

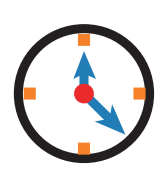


Worobey et al. (2014), Nature



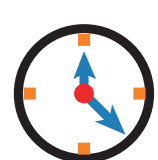
Rates of evolution can vary in the short term and long term





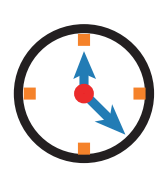
Mathematically clock models are functions that have divergence as input and time as output

- **Strict clock models** assume that evolution happens equally fast on each branch of a tree. Strict clocks are mostly used to study pathogens over rather short times (a few years)
- **Random clock models** allow different branches of a phylogenetic tree to have different rates (speed) of evolution. These are more prevalent when analyzing datasets that were sampled over longer time periods

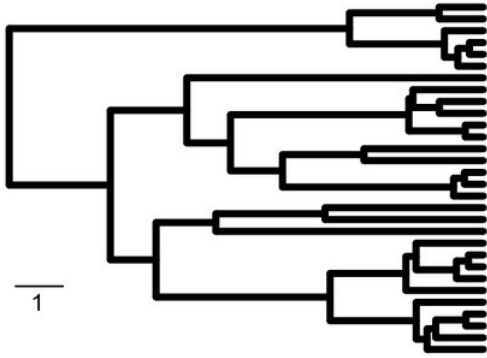


Random clock models can be separated into two classes

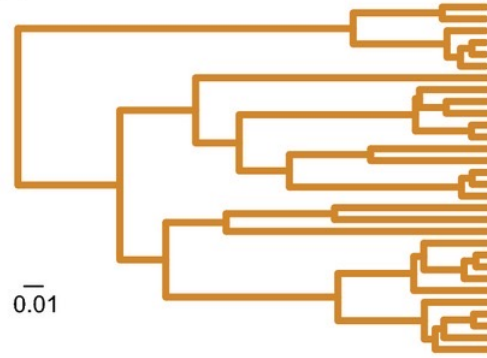
- **Local random clock models.** Clock rates change on a few branches in the tree only. Once they change, all the descendent branches will inherit the same rate
- **Uncorrelated clock models.** Clock rates can vary on each branch (completely uncorrelated). Each branch has a clock rate that is considered a random draw from some distribution (typically Exponential or lognormal).



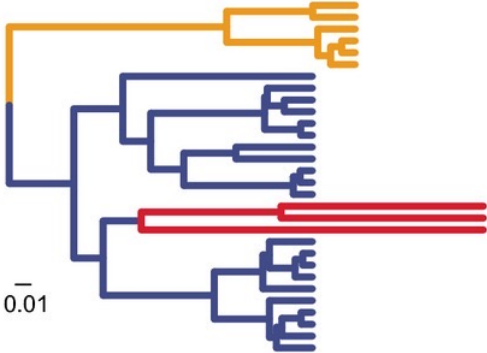
(a) Chronogram



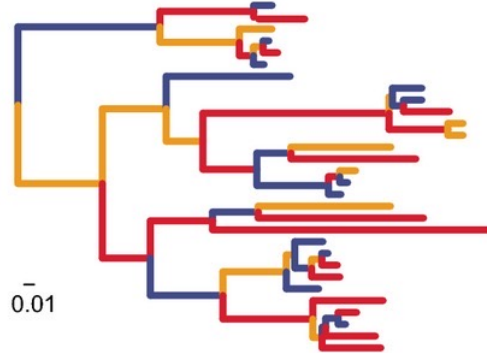
(b) Strict clock



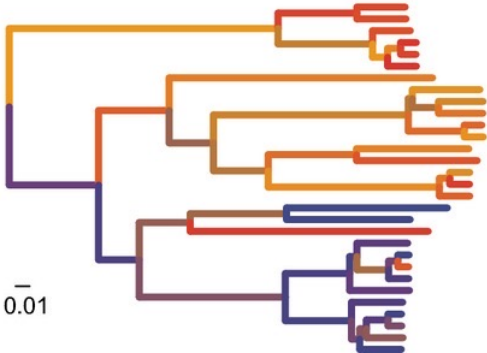
(c) Local multi-rate clock



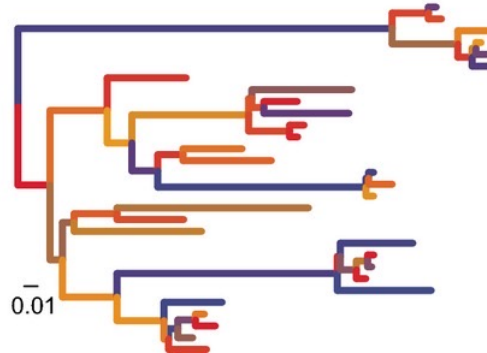
(d) Discrete multi-rate clock



(e) Autocorrelated relaxed clock

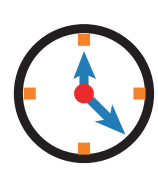


(f) Uncorrelated relaxed clock



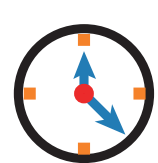
Molecular clock models map genetic divergence into time

- Clock models can account for variation in the speed of evolution across an evolutionary history.

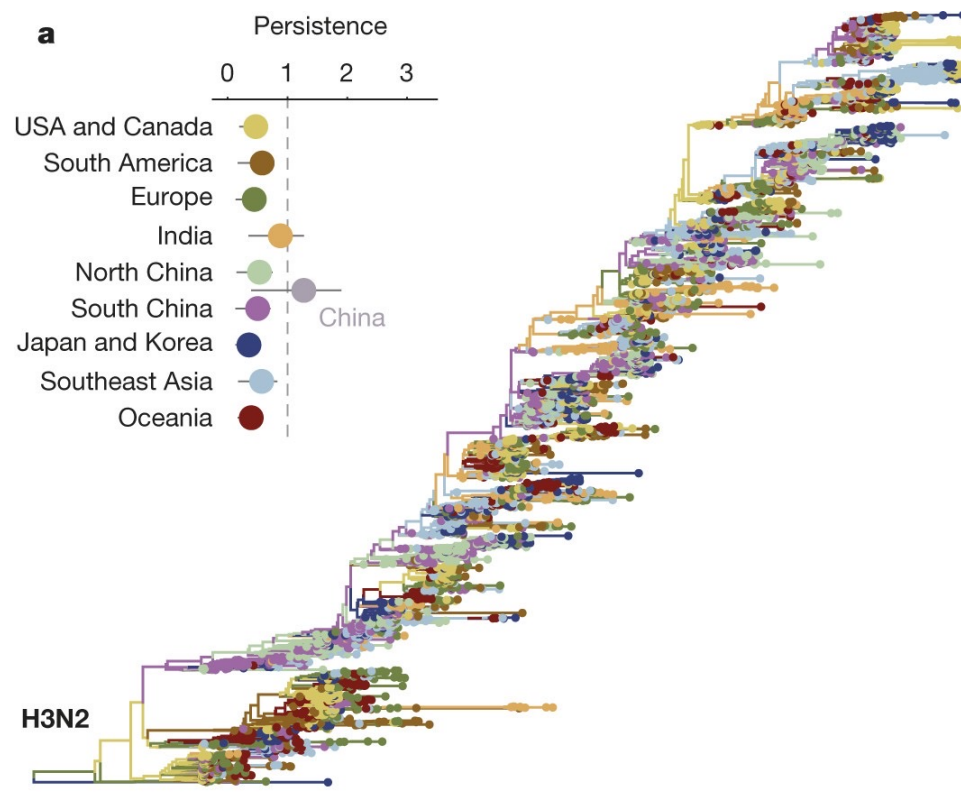


Where does the time information come from to inform the molecular clock?

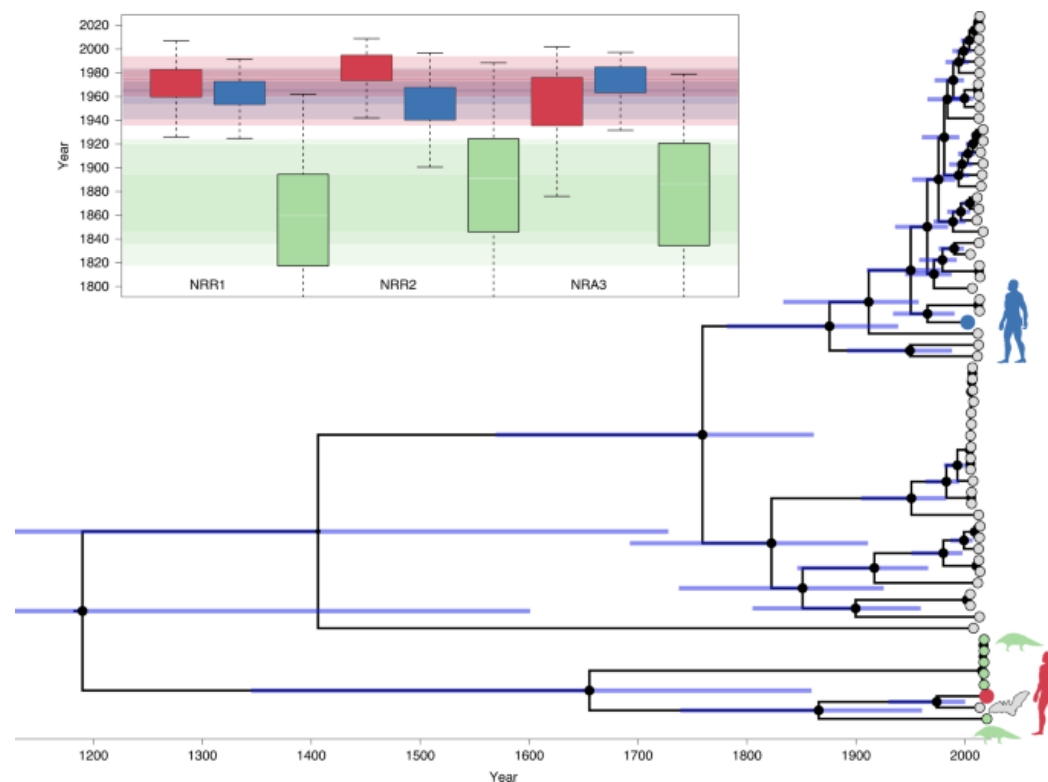
- Calibrations -> Knowing something about when two lineages shared a common ancestor.
- Sampling through time of “measurably evolving pathogens”.
- Just “knowing” the rate, that is from the prior.



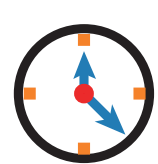
The time information should be in the same order of magnitude as the evolutionary history



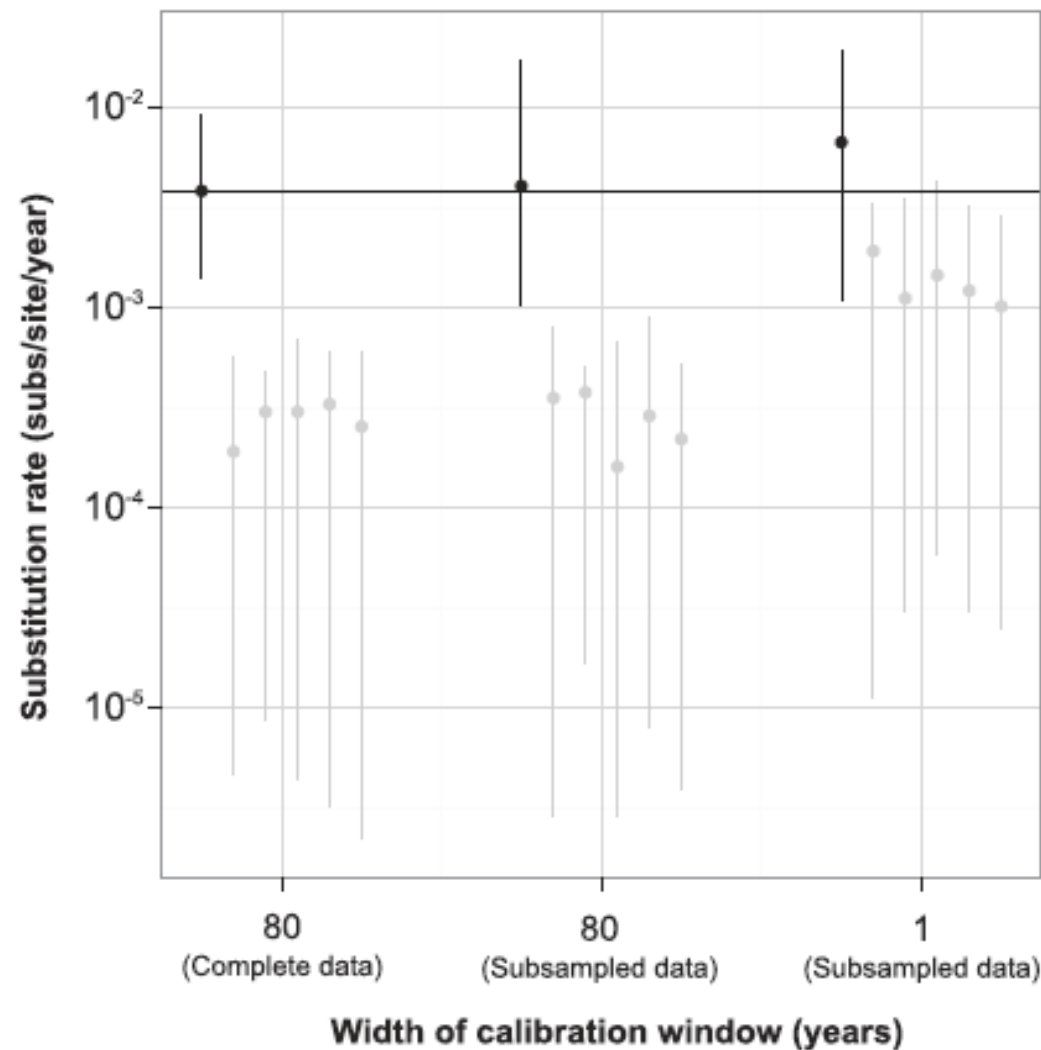
Bedford et al. (2015), Nature



Boni et al. (2020), Nat. Mic.



Is there enough signal to estimate evolutionary rates? Tip Randomization

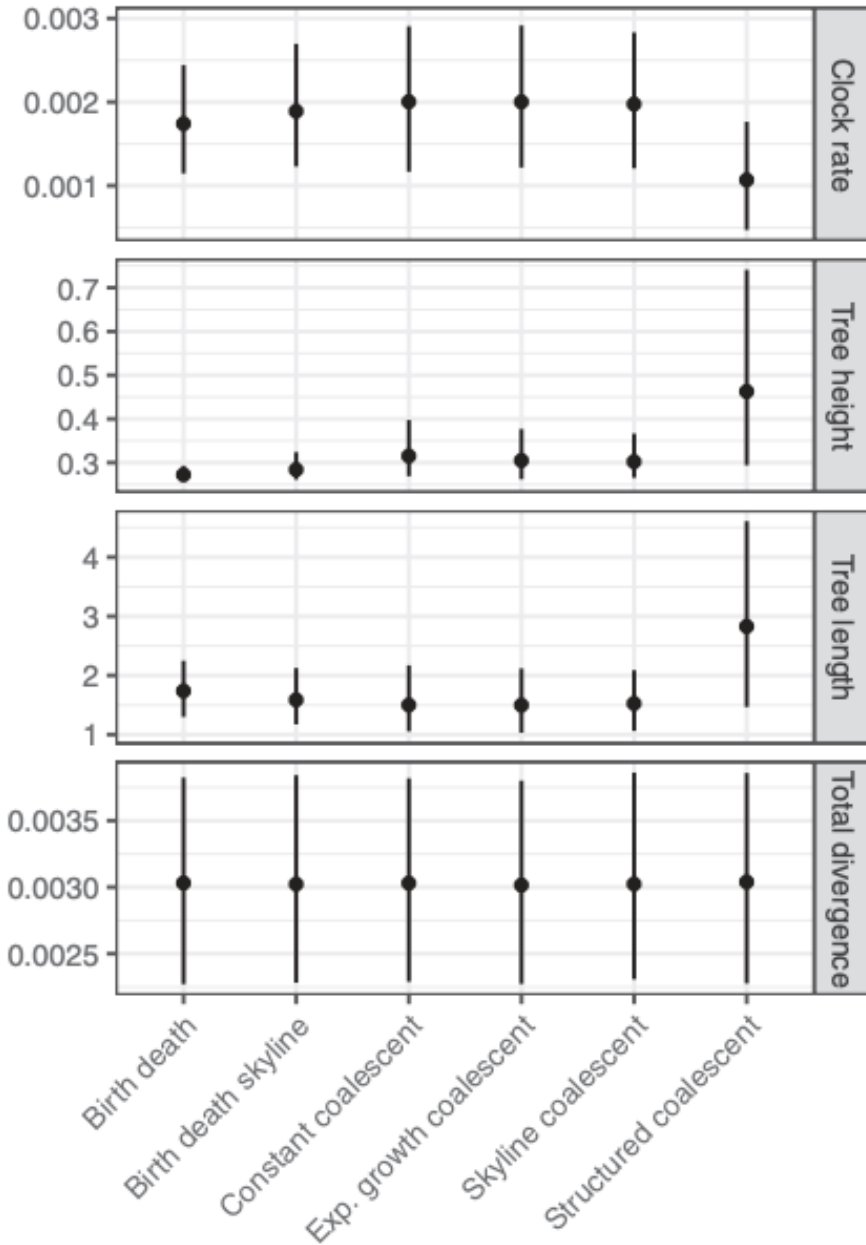


In the posterior probability, modelling the evolution of sequences feeds into the tree likelihood.

$$P(\text{Tree} \mid \text{Data}) = \frac{P(\text{Data} \mid \text{Tree}) P(\text{Tree}) P(\text{Model}) P(\text{Seq}) P(\text{Clock})}{P(\text{Data})}$$

The equation illustrates the components of the posterior probability in a Bayesian phylogenetic model. The numerator represents the joint probability of the data, tree, model, sequence, and clock, while the denominator represents the marginal probability of the data. The icons used are: a tree for the tree, a grid of colored dots for the data, a clock face for the clock, a sequence of colored dots for the sequence, and a model icon for the model.

B Sierra Leone



Model choices not directly related to clock models can impact rate estimates

Some reading material

- Accounting for codon positions:
<https://doi.org/10.1093/molbev/msj021>
- Overfitting site models is ok:
<https://www.nature.com/articles/s41467-019-08822-w>
- Posterior predictive simulations to evaluate clock signal:
<https://academic.oup.com/mbe/article/32/11/2986/981260>
- Time randomization to evaluate clock signal:
<https://academic.oup.com/mbe/article/32/7/1895/1016979>
- Rates of evolution in EBOV:
<https://www.nature.com/articles/nature19790>